The Crystal Structure of MgNb₁₄O₃₅F₂

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A phase analysis of the system MgF₂-Nb₂O₅ has revealed the existence of the compound MgNb₁₄O₃₅F₂. The crystal structure has been solved from three-dimensional Weissenberg data and refined by least-squares technique. The symmetry is monoclinic, space group C2/m and the unit cell dimensions: a = 20.628 Å; b = 3.825 Å; c = 19.098 Å and $\beta = 107.75^{\circ}$. The structure contains metal-oxygen (fluorine) octahedra which are linked by corners to form blocks measuring $5 \times 3 \times \infty$ octahedra. The blocks are mutually connected along planes of crystallographic shear by octahedra sharing edges. The structure represents the previously missing member n = 5 of a series of monoclinic block structures Me_{3n}X_{8n-3} found in the TiO₂-Nb₂O₅ system by Wadsley.

Introduction

The phase equilibrium relations and the crystal structures of the phases in the system $TiO_2-Nb_2O_5$ have been studied by Wadsley (1), (2), (3) and Roth (3). They found no large solubility of TiO_2 in Nb_2O_5 .

A phase analysis of the system MgF_{2} -mNb₂O₅ was, therefore, started to examine whether the conditions are the same in this system. The result of the phase analysis showed the existence of a phase with a composition corresponding to an *m* value of about 7. The Guinier X-ray powder pattern showed great resemblance to those of two substances, TiNb₂O₇ and Ti₂Nb₁₀O₂₉, belonging to a homologous series of shear structures, Me_{3n}X_{8n-3}, reported by Wadsley (1), (2). An X-ray crystallographic investigation was now started to find the structure and to establish the chemical character of the new compound.

Experimental

Crystals of the new compound were prepared by mixing of MgF₂ (Merck's reagent, pro analysi) and H-Nb₂O₅ (Kawecki, 99.99%) in a 1:7 ratio. The sample was heated in a sealed platinum tube at 1000°C for two days. The material thus obtained consisted of rod-shaped, colourless crystals.

The unit cell dimensions determined from a Guinier X-ray powder pattern (CuK α_1 radiation) were: $a = 20.628 \text{ Å} \pm 10; b = 3.825 \text{ Å} \pm 2; c = 19.098$

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Å \pm 10, and $\beta = 107.75^{\circ} \pm 2$. The indexing of the powder photograph is listed in Table I.

The observed density measured by the apparent loss of weight in benzene is 4.41 g cm⁻³. With two units of MgF₂-mNb₂O₅ per elementary cell this would correspond to a value of m = 6.94. The density value calculated for the stoichiometric formula MgNb₁₄O₃₅F₂, thus derived for the phase, is 4.45 g cm⁻³.

No real single crystal could be found. Thus, the intensity data were collected from a very small twin with a Weissenberg camera using filtered $CuK\alpha$ radiation. The h0l, h1l and h2l reflexions were recorded by multiple film technique. After separation of the two interpenetrating reciprocal lattices only the reflexions from one of the crystals were visually estimated by means of a standard scale. The 00l reflexions from the twin-individuals overlapped exactly. The contributions from these were determined by measurement of several equivalent noncoincident reflexions.

Structure Determination

The Weissenberg photographs showed monoclinic symmetry with systematic absences hkl when $h + k \neq 2n$. This condition gave the space group alternatives C2, Cm, and C2/m. The distribution of h0l and h2l intensities with due regard for observational errors and for the effects of thermal motion seemed to be identical. All the atoms were, therefore,

TABLE I The Guinier Powder Pattern of MgNb₁₄O₃₅F₂ (CuK α_1 Radiation)

Ι	$\sin^2 \theta_{obs}$	h k l	$\sin^2 \theta_{calc}$
w	0.00592	201	0.00592
vw	0.00618	200	0.00615
vw	0.00719	002	0.00717
w	0.01615	003	0.01614
m	0.02234	401	0.02234
m	0.02871	004	0.02869
vst	0.04206	110	0.04209
т	0.04282	111	0.04287
st	0.04482	005	0.04484
st	0.05033	602	0.05036
w	0.05116	601	0.05106
т	0.05308	311	0.05314
m	0.05566	312	0.05548
UW	0.06118	205	0.06111
w	0.07481	114	0.07483
st	0.07563	511	0.07571
w	0.07894	510	0.07898
vw	0.07952	313	0.07964
w	0.08339	606	0.08345
w	0.08922	802	0.08935
w	0.09040	803	0.09022
w	0.09531	314	0.09523
w	0.10844	604	0.10833
т	0.11063	711	0.11057
st	0.13884	803	0.13882

assumed to be situated in planes perpendicular to the y axis, a distance of b/2 apart. The higher symmetry, C2/m, was tentatively assumed for the structure investigation. The length of the b axis, 3.83 Å, suggested the structure to be built up of layers of polyhedra linked by sharing corners and edges.

The appearance of the Weissenberg photographs gave further support to the idea of a structural relationship existing between the investigated compound and the ternary titanium-niobium oxides in the homologous series $Me_{3n}X_{8n-3}$ reported by Wadsley (1), (2). The latter structures may be described in terms of blocks consisting of MeX₆ octahedra linked by corners as in the ReO₃ type. The blocks are of finite extension in two dimensions, measuring 3×3 and 3×4 octahedra and infinite in the third dimension. The blocks are joined by octahedra sharing edges in a complicated way (v. inf.).

The symmetry of $TiNb_2O_7$ and $Ti_2Nb_{10}O_{29}$ was given by Wadsley as A2/m. The space group of MgNb₁₄O₃₅F₂ is the same but the discussion of this compound will be in terms of the C-centered setting used in the International Tables of Crystallography. The c and b axes of the two titaniumniobium oxides are very nearly the same which reflects the common finite extension of three MeX₆ octahedra of the building blocks of these substances. The corresponding figures for the a and b axes of MgNb₁₄O₃₅F₂ have rather similar values suggesting blocks of this extension to be present also in this material. The extension in the third dimension of the three phases $(a\sin\beta \text{ and } c\sin\beta)$ increase regularly in the order 10.31 Å (TiNb₂O₇), 14.27 Å (Ti₂Nb₁₀O₂₉), and 18.19 Å (MgNb₁₄O₃₅F₂), which suggests that the block size of the latter is five octahedra in this direction.

The idea thus arrived at was tested by comparison of the observed unit cell dimensions for MgNb₁₄O₃₅F₂ with the corresponding data for the hypothetical member n = 5 of the monoclinic homologous series Me_{3n}X_{8n-3}:

	а	b	с	β
obs	20.628 Å	3.825 Å	19.098 Å	107.75°
calc	20.50 Å	3.80 Å	19.45 Å	108.5°

The point positions used in the space group C2/m are the following:

(0, 0, 0	$; \frac{1}{2}, \frac{1}{2}, 0$)+
4(i)	m	$x, 0, z; \bar{x}, 0, \bar{z},$
2(d)	2/m	$0, \frac{1}{2}, \frac{1}{2}$
2(c)	2/m	$0, 0, \frac{1}{2}$.

All the atoms except two metal and two nonmetal atoms of the hypothetical structure occupy 4(i) positions, while the remaining atoms occupy the special positions 2(c) and 2(d), respectively. The coordinate values for the various atoms were calculated by analogy with the data reported for the titanium-niobium oxides.

The preliminary structure factors calculated under the assumption of random occupancies of the metal as well as the nonmetal atom sites were found to be in acceptable agreement with the observed structure factors. Least-squares techniques were applied to refine the parameter values on the basis of the 216 independent reflexions from the h0l, h1l, and h2l layer lines. Owing to the relatively great number of parameters all temperature factors were fixed at 0.5 Å² for the metal atoms and 1.0 Å² for the anions, during the first stages of refinement. The R value dropped to 10.8%. Finally, individual isotropic temperature factors for the metal atoms were included in the refinement. The R factor obtained was 6.4%. The atomic parameters are given in Table II. The observed and calculated structure factors are listed in Table III.

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Atom	Position	x	у	Z	B	σΒ
Me(I)	4(<i>i</i>)	0.0630	0	0.0787	0.91	0.35
Me(II)	4(<i>i</i>)	0.1935	1	0.0791	2.61	0.44
Me(III)	4(<i>i</i>)	0.3736	$\frac{1}{2}$	0.0718	0.62	0.40
Me(IV)	4(<i>i</i>)	0.1208	0	0.2893	0.94	0.41
Me(V)	4 (<i>i</i>)	0.2515	$\frac{1}{2}$	0.2838	-0.29	0.33
Me(VI)	4(<i>i</i>)	0.4413	$\frac{1}{2}$	0.2971	0.10	0.42
Me(VII)	4(<i>i</i>)	0.1841	0	0.4991	0.20	0.51
Me(VIII)	2(c)	0	0	1	1.47	1.08
X(I)	4(<i>i</i>)	0.0857	$\frac{1}{2}$	0.0625		
X(II)	4 (<i>i</i>)	0.1565	0	0.0429		
X(III)	4(<i>i</i>)	0.2700	$\frac{1}{2}$	0.0681		
X(IV)	4 (<i>i</i>)	0.0878	0	0.1926		
X(V)	4(<i>i</i>)	0.2252	$\frac{1}{2}$	0.1873		
X(VI)	4(<i>i</i>)	0.4105	$\frac{1}{2}$	0.1665		
X(VII)	4 (<i>i</i>)	0.1428	1	0.2790		
X(VIII)	4 (<i>i</i>)	0.3413	$\frac{1}{2}$	0.2788		
X(IX)	4 (<i>i</i>)	0.4271	0	0.2664		
X(X)	4(i)	0.1588	0	0.3895		
X(XI)	4(i)	0.2904	$\frac{1}{2}$	0.3924		
X(XII)	4(<i>i</i>)	0.2261	0	0.2916		
X(XIII)	4 (<i>i</i>)	0.4692	1	0.0482		
X(XIV)	4 (<i>i</i>)	0.3598	0	0.0470		
X(XV)	4(<i>i</i>)	0.0896	0	0.5068		
X(XVI)	4(<i>i</i>)	0.4647	ł	0.3897		
X(XVII)	4(<i>i</i>)	0.0321	0	0.2829		
X(XVIII)	4(<i>i</i>)	0.2046	$\frac{1}{2}$	0.5228		
X(XIX)	2(<i>d</i>)	0	$\frac{1}{2}$	$\frac{1}{2}$		

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Atomic Parameters in MgNb₁₄O₃₅F₂—Space Group C2/m

Discussion

The structure determination fully confirms the assumption that $MgNb_{14}O_{35}F_2$ represents the n = 5 member of the monoclinic homologous series $Me_{3n}X_{8n-3}$. Thus, the structure consists of blocks of ReO₃ type which extend in the *ac* plane over 5×3 octahedra and are of infinite length along the *b* axis. The structural principles for the series $Me_{3n}X_{8n-3}$ are demonstrated by idealized drawings of the three compounds TiNb₂O₇, Ti₂Nb₁₀O₂₉, and MgNb₁₄O₃₅F₂ in Fig. 1.

The distortions of the octahedra are shown in Fig. 2 and the metal-anion distances are given in Table IV. In spite of a wide variation among the metal-anion distances the average value, 2.00 Å, is very similar to the distances found in H-Nb₂O₅, 1.99 Å (4), in N-Nb₂O₅, 2.01 Å, (5), and in Nb₃O₇F, 1.97 Å, (6). The anion-anion distances within the octahedra vary between 2.36-3.30 Å (σ around 0.15 Å). The shortest distances occur for shared edges, as was also observed in Ti₂Nb₁₀O₂₉ (2).

The accuracy of the atomic positional parameters and hence also of the interatomic distances is moderate which is obviously due partly to the fact that, because of the twinning an absorption correction could not be made and partly to the number of observed data being low in relation to the number of parameters to be determined. The effect of these shortcomings of the primary material is, however, more likely to be found in the "thermal parameters." As mentioned above the structure refinement had to be carried out with a common fixed value of the B parameter of the anions. The values obtained for the metal atoms vary considerably but the e.s.d.:s are also rather high. An interpretation of these values in terms of thermal motion seems unsound. This applies also to calculations of preferred occupancy of the various sites by the two metal atom species. This appreciation of the nonphysical significance of the *B*-parameter values is supported by some exploratory calculations.

It is interesting to compare the present structure

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н	κL	FO	FC	н	ΚL	FC	FC	н	ΚL	FO	FC	н	κL	۴O	FC
o	C 2	81	50	8	0 3	126	130	3	1 8	123	-139	0	29	590	- 605
C	0 3	178	172	× 8	07	227	252	3	19	202	199	0	2 10	403	381
0	04	429	· 390	10	0 -22	214	203	5	1 -11	617	-613	0	2 11	104	83
Ó	0 5	911	-857	10	0 - 17	316	-312	5	1 -7	164	-146	ō	2 13	82	72
Ō	0 6	225	-218	10	0 -13	198	-181	5	ī -6	382	375	õ	2 14	469	467
č	Č 7	199	-198	iõ	0 -12	476	468	ŝ	1 -5	150	155	Å	2 -6	184	1 75
Ċ	0 8	269	-262	10	0 -11	137	140	Ś	1 -4	95	106	Á	2 -1	186	-246
ō	0 9	836	-795	10	0 - 10	103	124	ŝ	1	152	145		2 -11	613	-529
č	č 10	472	444	10	0 -9	125	120	5	1 -2	337	388	Å.	2 -10	145	-120
ō	0 11	103	106	10	0 ÷8	429	464	ś	î _ī	574	- 473	Å	2 -7	340	-304
č	0 13	117	90	10	0 -7	251	-259	ś	îô	161	-155	Ă	2	165	310
ō	0 14	525	546	10	ñ - 6	132	-147	ś	îĩ	111	-113	Å	2 -5	151	167
2	0 -1	112	100	10	ñ -4	90	-88	ś	1 2	147	-150		2 - 5	171	04
2	õ õ	64	-82	10	ñ ñ	75	-94	6	1 3	321	-310		2 - 4	110	110
2	0 4	101	-109	îŭ	a i	164	-179	ś	1 4	179	187		2 - 2	427	A17
2	n e	156	162	10	0 2	564	553	é	1 9	591	636	, , , , , , , , , , , , , , , , , , ,	2 -2	105	_100
~	0 -11	122	-137	10	0 2	101	104	2	1 13	301	-306		2 -1	102	-199
7	0 -11	132	-132	10	0 4	101	104		1 13	362	-390	, ,	2 3	477	
7	0 -10	10	206	10	0 4	140	107	4	1 1	160	-103	Ŷ	2 1	122	-108
2	0 - 2	49	47	10		406	411	4	1 7	111	- 06	, e	2 8	414	447
7	0 -1	300	-345	10	0 7	221	-322		1 12	111	- 33		2 12	109	203
7	0 0	370	-343	10	í	351	- 355	11	1 -15	222	-240		2 13	118	-200
7	č 1	10	- 61	10		302	-309	11	1 -12	322	268	8	2 -12	143	-198
2		106	-109	10	0 10	300	212	섞	1 -11	109	160		2 -1	188	1/2
7		104	-108	12	0.6	210	280		1	115	040	8	2 -3	120	117
7	0 5	105	-104	17	0 -4	131	-137	11	1 -4	201	196	8	2 -2	212	-208
4	0 4	137	132	14	u I	120	109	11	1 -3	153	-806	10	2 -17	271	-271
		201	257	16	0 -14	520	496	11	1 -2	128	-170	10	2 - 13	147	-160
2	0 -21	214	-278	16	0 -10	212	214	11	1 -1	106	-101	10	2 -12	404	379
ç	0 -20	151	161	10	0 -9	386	-360	11	1 0	132	-143	10	2 -11	105	107
2	0 - 18	534	414	10	0 -5	244	~518	11	1 1	409	-405	10	2 -9	95	101
2	0 -11	241	-043	10	0 -4	247	243	11	1 2	415	405	10	Z -8	373	382
6	0 -10	147	-155	16	0 0	508	464	11	1 3	117	127	10	2 -7	220	-206
°,	9 -1	369	-351	16	0 5	493	-465	11	1 5	125	142	10	2 -3	599	-635
0	0 - 6	404	314	10	0 10	243	240	11	1 6	617	645	10	26	372	353
5	0 -5	181	1/6	22	0 -16	363	422	11	1 /	163	-181	10	2 7	275	-282
	0 -4	142	141	22	0 -12	112	122	11	1 11	433	-433	10	2 11	378	-315
÷.	0 -3	153	158	22	0 -11	371	-408	17	1 -14	287	297	12	2 -13	326	-309
2	0 -2	829	810	22	0 -7	293	-290	17	1 -13	141	187	12	2 -8	287	261
D	0 -1	213	-255	22	0 -6	365	351	17	1 -10	341	321	12	2 -4	275	232
,	6 6	122	-114	22	0 -2	413	350	17	1 -9	145	-125	12	2 - 3	189	-217
6	0 3	557	-535	22	0 3	373	-392	17	1 0	305	340	16	2 -14	446	433
0	0 6	79	-72	1	1 -5	529	-453	17	1 4	280	244	16	2 -10	256	Z4 4
0	0 /	213	-197	1	1 - 2	68	-104	17	15	283	-252	16	2 -9	299	-317
6	0 8	485	543	1	1 2	133	136	21	1 -11	336	-350	16	2 -8	117	-113
6	09	111	109	1	1 3	149	146	21	1 -6	446	418	16	2 -5	478	-445
6	0 10	107	97	1	14	293	302	21	1 -1	261	-268	16	2 -4	235	212
6	0 12	244	227	1	1 5	223	-235	21	1 3	345	-355	16	2.0	388	409
6	0 13	239	-227	1	18	98	-106	0	22	43	50	16	25	421	-407
8	0 -12	241	-248	ı	19	438	-474	0	23	109	125	16	29	187	-181
8	0 -7	207	211	1	1 14	258	267	C	24	280	282	16	2 10	208	216
8	0 -3	158	147	3	1 -6	137	-13C	C	25	655	-670	22	2 -11	336	-364
8	0 -2	251	-274	3	1 -5	132	124	0	26	159	-152	22	2 -7	269	- 26 1
8	0 0	69	- 57	3	1 -1	347	320	0	27	135	-131	22	2 -6	335	312
8	02	148	-145	3	14	209	-198	0	28	212	-199	22	2 -2	341	313

TABLE III Observed and Calculated Structure Factors for $MgNb_{14}O_{35}F_2$





FIG. 2. The crystal structure of MgNb₁₄O₃₅F₂ viewed along the b axis. \bigcirc Metal atoms at y = 0; \bullet metal atoms at $y = \frac{1}{2}$.

TABLE IV

Interatomic Distances in $MgNb_{14}O_{35}F_2-\!\!\!-\!\!\!-\!\!\!-$ Standard Deviations \pm 0.15 Å

Distance	Å	Mean value
Me(I)-2X(I)	2.01	· · · · · · · · · · · · · · · · · · ·
X(II)	2.23	
X(IV)	2.08	2.08
X'(XIII)	1.84	
X"(XIII)	2.31	
Me(II)-X(I)	2.15	
2X(II)	2.10	
X(III)	1.65	2.05
X(V)	1.97	
X(XIV)	2.32	
Me(III)-X(II)	2.09	
X(III)	2.12	
X(VI)	1.74	2.01
X(XIII)	2.15	
2X(XIV)	1.97	
Me(IV)–X(IV)	1.76	
2X(VII)	1.99	
X(X)	1.83	1.92
X(XII)	2.16	
X(XVII)	1.80	
Me(V)-X(V)	1.76	
X(VII)	2.22	
X(VIII)	1.88	1.97
X(XI)	1.98	
2X(XII)	2.00	
Me(VI)-X(VI)	2.38	
X(VIII)	1.98	

TABLE IV (continued)

INTERATOMIC DISTANCES IN MgNb14O35F2-
Standard Deviations ± 0.15 Å

Distance	Å	Mean value	
2X(IX)	2.00		
X(XVI)	1.69		
X(XVII)	1.94		
Me(VII)-X(X)	2.00		
X(XI)	1.98		
X(XV)	2.00	2.07	
2X'(XVIII)	1.98		
X"(XVIII)	2.45		
Me(VIII)-2X(XV)	1.82		
2X(XVI)	2.01	1.91	
2X(XIX)	1.91		

with that of $MoNb_{15}O_{40}F$ recently reported by Galy and Andersson (7). The latter is also a block-type structure containing the same type of units, measuring $5 \times 3 \times \infty$ octahedra. However, in this compound, the molybdenum atoms are inserted in tetrahedrally coordinated interstices at the junctions of four blocks. Thus, although the major structural units of the two compounds $MgNb_{14}O_{35}F_2$ and $MoNb_{15}O_{40}F$ are identical, they join rather differently.

The $Ti_2Nb_{10}O_{29}$ phase (2) and also the analogous binary niobium oxide $Nb_{12}O_{29}$ (8) exist in two

modifications, which bear a very close structural relation to each other. In addition to the monoclinic form described above, an orthorhombic structure exists which differs from the former essentially by the presence of mirror planes parallel to the ab plane in the C-centered description of the structure. The orthorhombic modifications of $Ti_2Nb_{10}O_{29}$ and Nb₁₂O₂₉ may be looked upon as representing the n = 4 members of an orthorhombic homologous series $Me_{3n}X_{8n-3}$, analogous to the monoclinic series discussed in this paper. No orthorhombic modification of TiNb₂O₇ (n = 3) has been observed. Attempts to prepare an orthorhombic version of $MgNb_{14}O_{35}F_2$ by heat treatment at different temperatures have so far been without success. It is interesting to observe, however, that the twinning always found in the monoclinic crystals occurs on the *ab* plane.

Detailed descriptions of the structural principles involved in this family of shear structures have been given recently (9), (10) and will not be repeated here.

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